

Unit 2 Word Problems Review

- ① Let x represent the number.

$$\begin{aligned} 5x + 7 &= 27 \\ 5x &= 27 - 7 \\ \frac{5x}{5} &= \frac{20}{5} \\ x &= 4 \end{aligned}$$

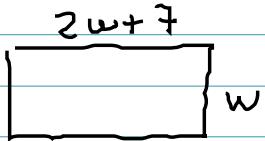
∴ The number is 4.

- ② Let b represent the # of boys
 Let $30-b$ represent the # of girls
 (# girls \leq 3 less than double boys)

$$\begin{aligned} 30 - b &= 2b - 3 \\ -b - 2b &= -3 - 30 \\ \frac{-3b}{-3} &= \frac{-33}{-3} \\ b &= 11 \end{aligned} \quad \left. \begin{aligned} 30 - b &= 30 - 11 \\ &= 19 \end{aligned} \right\}$$

∴ There are 11 boys and 19 girls.

- ③



$$\begin{aligned} 2w + 2(2w+7) &= 86 \\ 2w + 4w + 14 &= 86 \\ 6w &= 86 - 14 \\ \frac{6w}{6} &= \frac{72}{6} \\ w &= 12 \end{aligned} \quad \left. \begin{aligned} 2w+7 &= 2(12)+7 \\ &= 24+7 \\ &= 31 \end{aligned} \right\}$$

∴ The rectangle is 12cm by 31cm

- ④ Let n represent the # of nickels.
 Let $32-n$ represent the # of dimes.

$$0.05n + 0.10(32-n) = 2.80$$

$$0.05n + 3.2 - 0.10n = 2.80$$

$$0.05n - 0.10n = 2.80 - 3.2$$

$$\underline{-0.05n} \quad \underline{-0.10n}$$

$$n = 8$$

$$\begin{aligned} \text{dimes} &= 32 - n \\ &= 32 - 8 \\ &= 24 \end{aligned}$$

∴ There are 8 nickels and 24 dimes.

- ⑤ Let s represent the ^{price} of small deluxe pizzas (\$)
 Let $s+4$ represent the price of a large deluxe pizza (\$)

$$5s + 1(s+4) = 38.50$$

$$5s + s + 4 = 38.50$$

$$6s = 38.50 - 4$$

$$\underline{6s} \quad \underline{34.50}$$

$$s = 5.75$$

$$\begin{aligned} \text{large} &= s + 4 \\ &= 5.75 + 4 \\ &= 9.75 \end{aligned}$$

∴ The small pizza is \$5.75 and the large is \$9.75

- ⑥ Let $x, x+1, x+2$ represent the ages (yrs).

$$x + x+1 + x+2 = 42$$

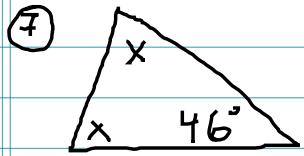
$$x + x + 2 = 42 - 2 - 1$$

$$\underline{3x} \quad \underline{3}$$

$$x = 13$$

$$\begin{aligned} x+1 &= 14 \\ x+2 &= 15 \end{aligned}$$

∴ Their ages are 13, 14, and 15.



$$\begin{aligned} x + x + 46 &= 180 \\ x + x &= 180 - 46 \\ \frac{2x}{2} &= \frac{134}{2} \\ x &= 67 \end{aligned}$$

∴ The equal angles are 67° .

- ⑧ Let q represent the # of quarters.
Let $q+5$ represent the # of nickels.

Let $40-q-(q+5)$ represent the # of dimes.
 $40 - q - q - 5$
 $= 35 - 2q$

$$\begin{aligned} 0.25q + 0.05(q+5) + 0.10(35-2q) &= 5.25 \\ 0.25q + 0.05q + 0.25 + 3.5 - 0.2q &= 5.25 \\ 0.25q + 0.05q - 0.2q &= 5.25 - 0.25 - 3.5 \\ \frac{0.1q}{0.1} &= 1.5 \\ q &= 15 \end{aligned}$$

Then:

$$\text{nickels} \cdot q + 5 = 15 + 5 \\ = 20$$

$$\begin{aligned} \text{dimes} &= 35 - 2q \\ &= 35 - 2(15) \\ &= 35 - 30 \\ &= 5 \end{aligned}$$

∴ There are 15 quarters, 20 nickels,
and 5 dimes.

④ Let x represent the # of upgrades Campbell sells.

$$\$ \text{by hours} + \$ \text{upgrades} = 640$$

$$9.10(40) + 12(x) = 640$$

$$364 + 12x = 640$$

$$12x = 640 - 364$$

$$\frac{12x}{12} = \frac{276}{12}$$

$$x = 23$$

∴ HC needs to sell 23 upgrades.

⑤ Let x represent the number.

$$\frac{(2)(5x - 20)}{2} = 15$$

$$5x - 20 = 30$$

$$5x = 30 + 20$$

$$5x = 50$$

$$x = 10$$

∴ The number is 10.

⑥ Let x represent the number

$$3(x + 4) = 2x$$

$$3x + 12 = 2x$$

$$3x - 2x = -12$$

$$x = -12$$

∴ The number is -12.

(12) Let x represent the number

$$(13) \frac{x}{z} = x + 9^{(3)}$$

$$x = 3x + 27$$

$$x - 3x = 27$$

$$\frac{-2x}{-2} = \frac{27}{-2}$$

$$x = \frac{-27}{2}$$

∴ The number is $-\frac{27}{2}$.

(13) Let x represent the smallest angle (${}^\circ$).

Let $x+40$ represent the second angle (${}^\circ$).

Let $\frac{x+x+40}{z}$ represent the third angle (${}^\circ$)

$$x + x + 40 + \frac{x+x+40}{z} = 180$$

$$(2) 2x + 40 + \frac{(2x+40)}{z} = 180^{(2)}$$

$$4x + 80 + 2x + 40 = 360$$

$$4x + 2x = 360 - 80 - 40$$

$$\frac{6x}{6} = \frac{240}{6}$$

$$x = 40$$

$$\begin{aligned} \text{2nd angle} &= x + 40 \\ &= 40 + 40 \\ &= 80 \end{aligned}$$

$$\begin{aligned} \text{3rd angle} &= \frac{x+x+40}{z} \\ &= \frac{40+40+40}{z} \\ &= 60 \end{aligned}$$

∴ The angles are $40^\circ, 60^\circ$ and 80°

⑭ Let $2x+1$ represent the first #.
 Let $2x+3$ represent the next #.

$$\begin{aligned} 2x+1 + 2x+3 &= 160 \\ 2x+2x &= 160 - 1 - 3 \\ 4x &= 156 \\ \frac{4x}{4} &= \frac{156}{4} \\ x &= 39 \end{aligned}$$

$\rightarrow \text{first } \# = 2x+1$
 $= 2(39)+1$
 $= 79$
 $\text{second } \# = 2x+3$
 $= 2(39)+3$
 $= 81$

∴ The numbers are 79 and 81.

⑮ Let x represent the # of dimes.
 Let $200-x$ represent the # of quarters.

$$\begin{aligned} 0.10x + 0.25(200-x) &= 42.50 \\ 0.10x + 50 - 0.25x &= 42.50 \\ 0.10x - 0.25x &= 42.50 - 50 \\ -0.15x &= -7.5 \\ \frac{-0.15x}{-0.15} &= \frac{-7.5}{-0.15} \\ x &= 50 \end{aligned}$$

$$\begin{aligned} \text{Quarters} &= 200-x \\ &= 200-50 \\ &= 150 \end{aligned}$$

∴ There are 50 dimes and 150 quarters.

⑯ Let x represent the # of \$10 bills.
 Let $125-x$ represent the # of \$20 bills.

$$\begin{aligned} 10x + 20(125-x) &= 1650 \\ 10x + 2500 - 20x &= 1650 \\ 10x - 20x &= 1650 - 2500 \\ -10x &= -850 \\ \frac{-10x}{-10} &= \frac{-850}{-10} \\ x &= 85 \end{aligned}$$

$\rightarrow \$20 \text{ bills} = 125-x$
 $= 125-85$
 $= 40$

∴ There are 85 \$10 bills and 40 \$20 bills.

(17) Let x represent the # of quarters.
Let λ represent the # of ~~dimes~~ nickels.
Let $53 - 2x$ represent the # of dimes

$$0.25x + 0.05x + 0.10(53 - 2x) = 6.80$$

$$0.25x + 0.05x + 5.3 - 0.2x = 6.80$$

$$0.25x + 0.05x - 0.2x = 6.8 - 5.3$$

$$\frac{0.1x}{0.1} = \frac{1.50}{0.1}$$

$$x = 15$$

$$\begin{aligned}\text{dimes} &= 53 - 2x \\ &= 53 - 2(15) \\ &= 53 - 30 \\ &= 23\end{aligned}$$

∴ There are 15 quarters, 15 nickels, and 23 dimes