

Basic Skills Review Stations

Station	Answer(s)	For administrative use only
R	a) $-\frac{7}{30}$ b) $\frac{5}{12}$ c) $-\frac{1}{10}$ d) 8 e) $\frac{8}{9}$	
E ₁	a) $\frac{15}{2} - \frac{23w}{5}$ b) $7x - 14$	
V	a) $x = 3$ b) $y = \frac{13}{5}$ c) $m = 7$	
I	a) $(1, -10)$ b) $(2, -3)$	
E ₂	a) $\frac{5x^5}{6}$ b) $32x^7y''$ c) $\frac{15}{2x^2}$ d) $5xy^2$ e) $10b^2 + b - 3$ f) $x^2 - 12x + 36$ g) $9m^2 - 4$	
W	a) $7t^2(1-2t)$ b) $2x(2y-z+5)$ c) $(5x-3)(5x+3)$ d) $(a-2)(a-5)$ e) $(2m-3)(3m+4)$ f) $(4z-3)^2$	

1. Evaluate. Answer should be a number.

a) $\frac{-5}{6} + \frac{3}{5}$ common denominator
 [LCD = 30]
 $= \frac{-5 \cdot 5}{6 \cdot 5} + \frac{3 \cdot 6}{5 \cdot 6}$
 $= \frac{-25}{30} + \frac{18}{30}$ [Equivalent Fractions]
 $= \frac{-25 + 18}{30}$

c) $\frac{-3}{2} \left(\frac{8}{15} \right)$ reduce when multiplying
 [Look for common factors between any numerator & denominator.]
 $= \frac{-1}{10}$

b) $\frac{1}{3} - \left(\frac{-1}{12} \right)$ common denominator
 [Simplify signs]
 $= \frac{1}{3} + \frac{1}{12}$
 $= \frac{4}{12} + \frac{1}{12}$
 $= \frac{5}{12}$

d) $\frac{1}{4} \div \frac{1}{32}$ change division to multiplication
 $= \frac{1}{4} \times 32$
 $= 8$

e) $\frac{5}{2} + \frac{2}{2} - \left(\frac{2}{6} \times \frac{1}{3} \right)$ BEDMAS!
 [Start with any reducing.]
 $= \frac{1}{2} + \frac{1}{2} - \left(\frac{1}{3} \times \frac{1}{3} \right)$
 $= 1 - \frac{1}{9}$
 $= \frac{9}{9} - \frac{1}{9}$
 $= \frac{8}{9}$

2. Simplify. Answer will have variables.

$$\begin{aligned} \text{a) } & -\frac{1}{4}(4w-6) - \frac{3}{5}(6w-10) \quad [\text{Distributive Property}] \\ & = \frac{-1}{4_1}(4w) - \frac{1}{4_2}(-6) - \frac{3}{5}(6w) - \frac{3}{5}(-10) \\ & = -w + \frac{3}{2} - \frac{18w}{5} + 6 \quad [\text{Collect Like Terms}] \\ & = -w - \frac{18w}{5} + \frac{3}{2} + 6 \\ & = \frac{-5w}{5} - \frac{18w}{5} + \frac{3}{2} + \frac{12}{2} \\ & = \frac{-23w}{5} + \frac{15}{2} \\ & = \frac{15}{2} - \frac{23w}{5} \end{aligned}$$

everything in the brackets is multiplied by -1

$$\begin{aligned} \text{b) } & 4x - (3x-1) - 3 + 6(x-2) \\ & = 4x - 3x + 1 - 3 + 6x - 12 \\ & = 4x - 3x + 6x + 1 - 3 - 12 \\ & = 7x - 14 \end{aligned}$$

3. Solve. Find the value of the variable that makes the statement true.

a) $5(x-3) - 2x = -6$ [Expand and Simplify before Solving]

$$5x - 15 - 2x = -6$$

$$3x - 15 = -6$$
 [Isolate x]

$$3x - 15 + 15 = -6 + 15$$

$$3x = 9$$

$$\frac{3x}{3} = \frac{9}{3}$$

$$x = 3$$

b) $4y - (3y - 1) = 6(y - 2)$

$$4y - 3y + 1 = 6y - 12$$

$$y + 1 = 6y - 12$$

$$1 + 12 = 6y - y$$
 [Variables on one side, constants on other side]

$$13 = 5y$$

$$\frac{13}{5} = y$$

c) $\frac{2m+1}{3} - \frac{m+1}{4} = 3$

[Clear the denominators].

$$\overset{4}{\cancel{12}} \left[\frac{2m+1}{\cancel{3}1} \right] - \overset{3}{\cancel{12}} \left[\frac{m+1}{\cancel{4}1} \right] = 12(3)$$

LCM = 12 Maintain balance.

$$4(2m+1) - 3(m+1) = 36$$

$$8m + 4 - 3m - 3 = 36$$

$$5m + 1 = 36$$

$$5m = 35$$

$$m = 7$$

→ two or more equations

4.a) Solve the system by the method of substitution.

$$\textcircled{1} 11x - y = 21$$

$$\textcircled{2} 9x + 2y = -11$$

→ isolate a variable, then substitute expression into other equation.

* The only good choice for isolation is "y" in $\textcircled{1}$ since its coefficient is 1.

$$\text{In } \textcircled{1}: 11x - 21 = y$$

$$\begin{aligned} \text{Sub. } y \text{ into } \textcircled{2}: & 9x + 2(11x - 21) = -11 \\ & 9x + 22x - 42 = -11 \\ & 31x = 31 \\ & x = 1 \end{aligned}$$

$$\begin{aligned} \text{Sub. } x \text{ into } \textcircled{1}: & 11(1) - y = 21 \\ & 11 - 21 = y \\ & -10 = y \end{aligned}$$

∴ The solution is $(1, -10)$.

b) Solve the system by the method of elimination.

→ Multiple one or both equations such that coefficients of x or y are equal. Add or subtract the new equations to eliminate one of the variables.

$$\textcircled{1} x + 2y = -4$$

$$\textcircled{2} 3x - 4y = 18$$

$$\times 3 \textcircled{1} 3x + 6y = -12$$

$$\underline{- \textcircled{2} 3x - 4y = 18}$$

$$10y = -30$$

$$y = -3$$

$$\begin{aligned} \text{Sub. } y \text{ into } \textcircled{1}: & x + 2(-3) = -4 \\ & x - 6 = -4 \\ & x = 2 \end{aligned}$$

∴ The solution is $(2, -3)$.

5. Simplify.

$$a) \left(\frac{2x^2}{3}\right)\left(\frac{5x^3}{4^2}\right)$$

$$= \frac{5x^5}{6}$$

TIP: Reduce common factors between numerators & denominators.

PRODUCT RULE

$$x^m \cdot x^n$$

$$= x^{m+n}$$

$$b) (2x^2y^3)^3(4xy^2)$$

$$= (2^3x^6y^9)(4xy^2)$$

$$= (8x^6y^9)(4xy^2)$$

$$= 32x^7y^{11}$$

POWER OF A POWER RULE

$$(x^m)^n$$

$$= x^{mn}$$

$$c) \left(\frac{3x}{2}\right) \div \left(\frac{x^3}{5}\right)$$

$$= \left(\frac{3x}{2}\right)\left(\frac{5}{x^3}\right)$$

$$= \frac{15x}{2x^3}$$

$$= \frac{15}{2x^2}$$

Multiply by the reciprocal.

Notice there are more factors of x in the denom.

$$d) (25x^3y^3) \div (5x^2y)$$

$$= \frac{25x^3y^3}{5x^2y}$$

$$= 5xy^2$$

QUOTIENT RULE

$$x^m \div x^n$$

$$= x^{m-n}$$

Expanding \rightarrow Multiplying ... Product of Terms \rightarrow Sum of Terms

$$e) (2b-1)(5b+3)$$

Distributive Property twice.

$$= 10b^2 + 6b - 5b - 3$$

$$= 10b^2 + b - 3$$

$$f) (x-6)^2$$

$$= x^2 - 12x + 36$$

Squaring a binomial results in a Perfect Square Trinomial.

$$(x-6)^2$$

$$= (x-6)(x-6)$$

$$g) (3m-2)(3m+2)$$

$$= 9m^2 - 4$$

Difference of Squares

Opposite of expanding.

Sum of terms \rightarrow Product of terms.

6. Factor.

a) $7t^2 - 14t^3$ Always look for a common factor first.

$$= 7t^2(1 - 2t)$$

GCF = $7t^2$

Divide the polynomial by the GCF to get the 2nd factor.

b) $4xy - 2xz + 10x$ GCF = $2x$

$$= 2x(2y - z + 5)$$

c) $25x^2 - 9$ Difference of Squares

$$= (5x - 3)(5x + 3)$$

d) $a^2 - 7a + 10$ Simple Trinomial

$$= (a - 2)(a - 5)$$

M 10

A -7

N -2, -5

e) $6m^2 - m - 12$

$$= (2m - 3)(3m + 4)$$

Complex Trinomial

M -72

A -1

N -9, 8

\leftarrow This is "a" times "c", "6" times "-12".

\leftarrow This is "b".

$$\frac{6}{-9}, \frac{6}{8}$$

\leftarrow Put the "a" value in the numerator.

\leftarrow Put your numbers in the denom.

$$= \frac{6 \div 3}{-9 \div 3}, \frac{6 \div 2}{8 \div 2}$$

\leftarrow Reduce the fractions.

$$= \frac{2}{-3}, \frac{3}{4}$$

1st factor 2nd factor

\leftarrow These are the values that go into each factor.

Keep the signs exactly the same. Order matters!

f) $16z^2 - 24z + 9$

$$= (4z - 3)^2$$

Perfect Square Trinomial

Remember the pattern?

$$\sqrt{16z^2}$$

$$= 4z$$

$$\sqrt{9}$$

$$= 3$$

Double the product of these square roots gives $24z$.

Remember \rightarrow When you square a binomial you get a perfect square trinomial!