

4.1 Exponent Rules

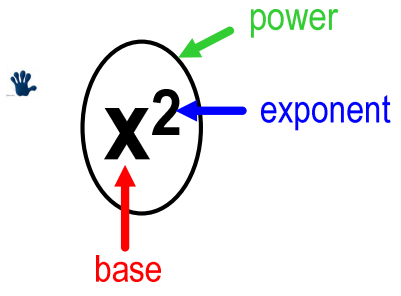
In multiplication, the terms that are multiplied together are called the base
 A repeated multiplication of equal factors can be expressed as a power

- $2 \times 2 \times 2 \times 2 \times 2 =$
- 2 is the base
 - 5 is the exponent
 - 2^5 is the power

$3 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3 = 3^9$

$(-5)(-5)(-5)(-5)(-5) = (-5)^5$

$\underbrace{a \times a \times a \times a \times a \times a \times a \times a \times a \dots \times a}_{n \text{ times}} = a^n$



Apr 22-11:11 AM

Remember exponents affect ONLY the number it touches in a power:

$-2^3 = -2 \times 2 \times 2$ $= -8$	$(-2)^3 = (-2)(-2)(-2)$ $= -8$
$-5^2 = -5 \times 5$ $= -25$	$(-5)^2 = (-5)(-5)$ $= 25$

Very important when you have neg. base and even exponent

Also Remember

If you can't see an exponent it is 1

ie $3 = 3^1$ $x = x^1$

Apr 28-8:57 AM

The Exponent RulesCollecting Like terms!

You can only add/subtract powers when both the base and the exponents are the same! (like terms!)

$$a^n + a^m = a^n + a^m$$

$$\text{but } a^2 + a^2 = 2a^2$$

CAN'T COMBINE

MULTIPLYING powers with the SAME baseKeep the base the same and **ADD** the exponents

$$a^p \times a^r = a^{p+r}$$

Example

$$(2^3)(2^7) \\ = 2^{10}$$

DIVIDING powers with the SAME baseKeep the base the same and **SUBTRACT** the exponents

$$a^p \div a^r = a^{p-r}$$

Example

$$\frac{3^6}{3^4} = 3^2$$

Power of a powerKeep the base the same and **MULTIPLY** the exponents

$$(a^p)^r = a^{p \times r}$$

Example

$$(5^2)^3 \\ = 5^6$$

Apr 22-12:10 PM

Ex 1. Write as a single power then evaluate the following:

$$\begin{array}{l} \text{a) } 3^2 \times 3^4 \\ = 3^6 \\ = 729 \end{array}$$

$$\begin{array}{l} \text{b) } 2^8 \div 2^5 \\ = 2^3 \\ = 8 \end{array}$$

$$\begin{array}{l} \text{c) } (0.1)^2 \times (0.1) \\ = (0.1)^3 \\ = 0.001 \end{array}$$

$$\begin{array}{l} \text{d) } (-5)^2 \times (-5) \\ = (-5)^3 \\ = -125 \end{array}$$

$$\begin{array}{l} \text{e) } (-5)^2 \times (-5)^2 \\ = (-5)^4 \\ = 625 \end{array}$$

Apr 28-9:52 AM

WORKBREAK - Simplify then evaluate

$$\begin{aligned} \text{a) } &= 4^2 \times 4^3 \\ &= 4^5 \\ &= 1024 \end{aligned}$$



$$\begin{aligned} \text{b) } &8^{16} \div 8^{13} \\ &= 8^3 \\ &= 512 \end{aligned}$$



$$\begin{aligned} \text{c) } &(5^2)^3 \\ &= 5^6 \\ &= 15625 \end{aligned}$$



$$\begin{aligned} \text{d) } &(4^1)^5 \\ &= 4^5 \\ &= 1024 \end{aligned}$$



$$\begin{aligned} \text{e) } &10^{12} \div 10^4 \div 10^5 \\ &= 10^3 \\ &= 1000 \end{aligned}$$



$$\begin{aligned} \text{f) } &(-3)^3 \times (-3)^2 \\ &= (-3)^5 \\ &= -243 \end{aligned}$$



$$\begin{aligned} \text{g) } &(-5)^4 \div (-5)^2 \\ &= (-5)^2 \\ &= 25 \end{aligned}$$



$$\begin{aligned} \text{h) } &2^3 \times 3^2 \\ &= 8 \times 9 \\ &= 72 \end{aligned}$$

NOT same
base, can't
use exp. laws



$$\begin{aligned} \text{i) } &6^2 + 6^3 \\ &= 36 + 216 \\ &= 252 \end{aligned}$$

NOT
multiplication
can't use
exp. laws



Apr 22-12:16 PM

Extend the rules:Power of a product:

Keep the base the same and the exponent goes to each part of the base

$$(ab)^m = a^m b^m$$

Example

$$\begin{aligned} (x^2 y^3)^3 &= x^{2 \times 3} y^3 \\ &= x^6 y^3 \end{aligned}$$

Power of a quotient:

Keep the base the same and the exponent goes to each part of the base

$$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$$

Example

$$\left(\frac{2}{7}\right)^2 = \frac{2^2}{7^2}$$

Putting the rules together:

Ex: Simplify

$$\text{a) } \left(\frac{2}{3}\right)^7 \div \left(\frac{2}{3}\right)^5$$

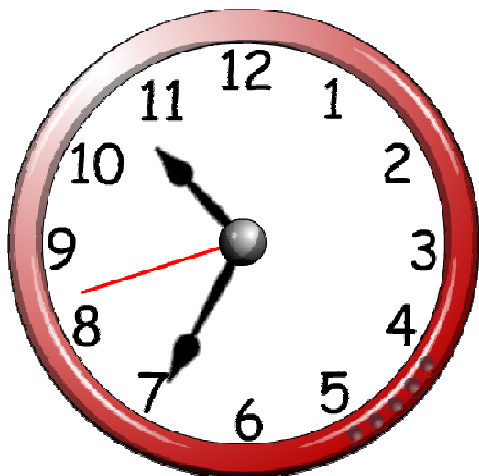
BONUS

$$\text{b) } \left(\frac{1}{3^2}\right)^4 = \frac{1^4}{3^8}$$

Apr 28-9:11 AM

Homework:

p. 360# 1-3 eoo, 5 eoo, 8, 9,
16b, 17



eoo?
"Every other one!"

Apr 22-1:07 PM